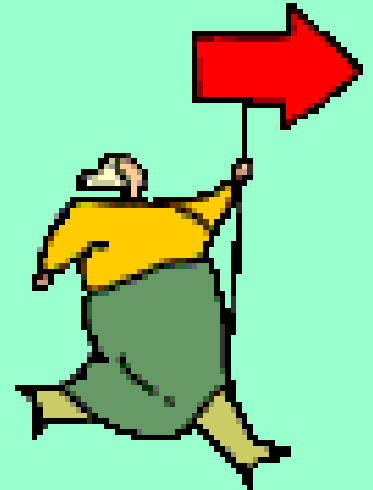


9.

Graph of $f(x+a)$



Graph of $f(x + a)$

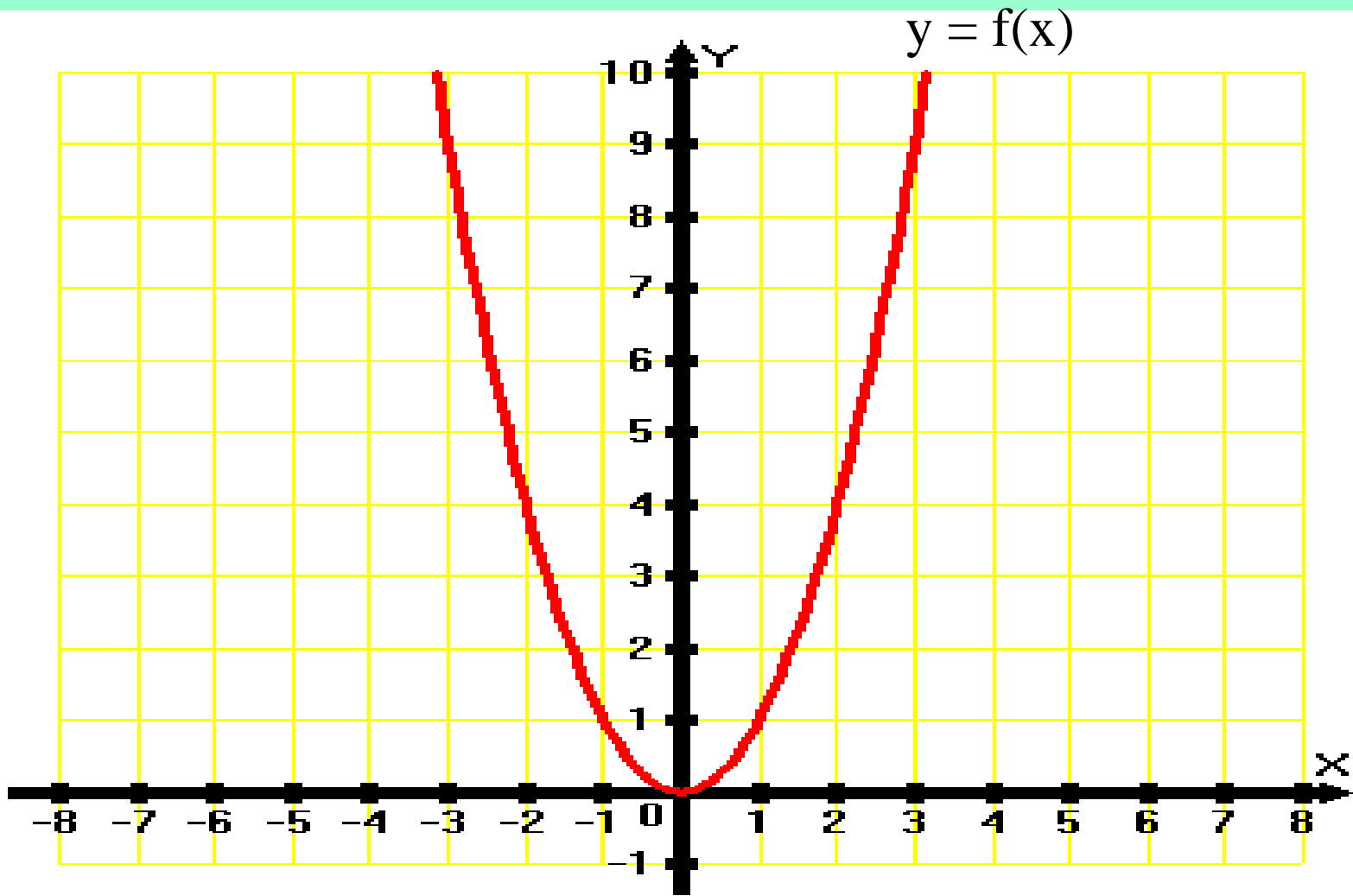
Having looked at $f(x) + a$, we can now look at another transformation.

Whereas $f(x) + a$ produced changes in the y direction, we are now going to look at changes in the x -direction.

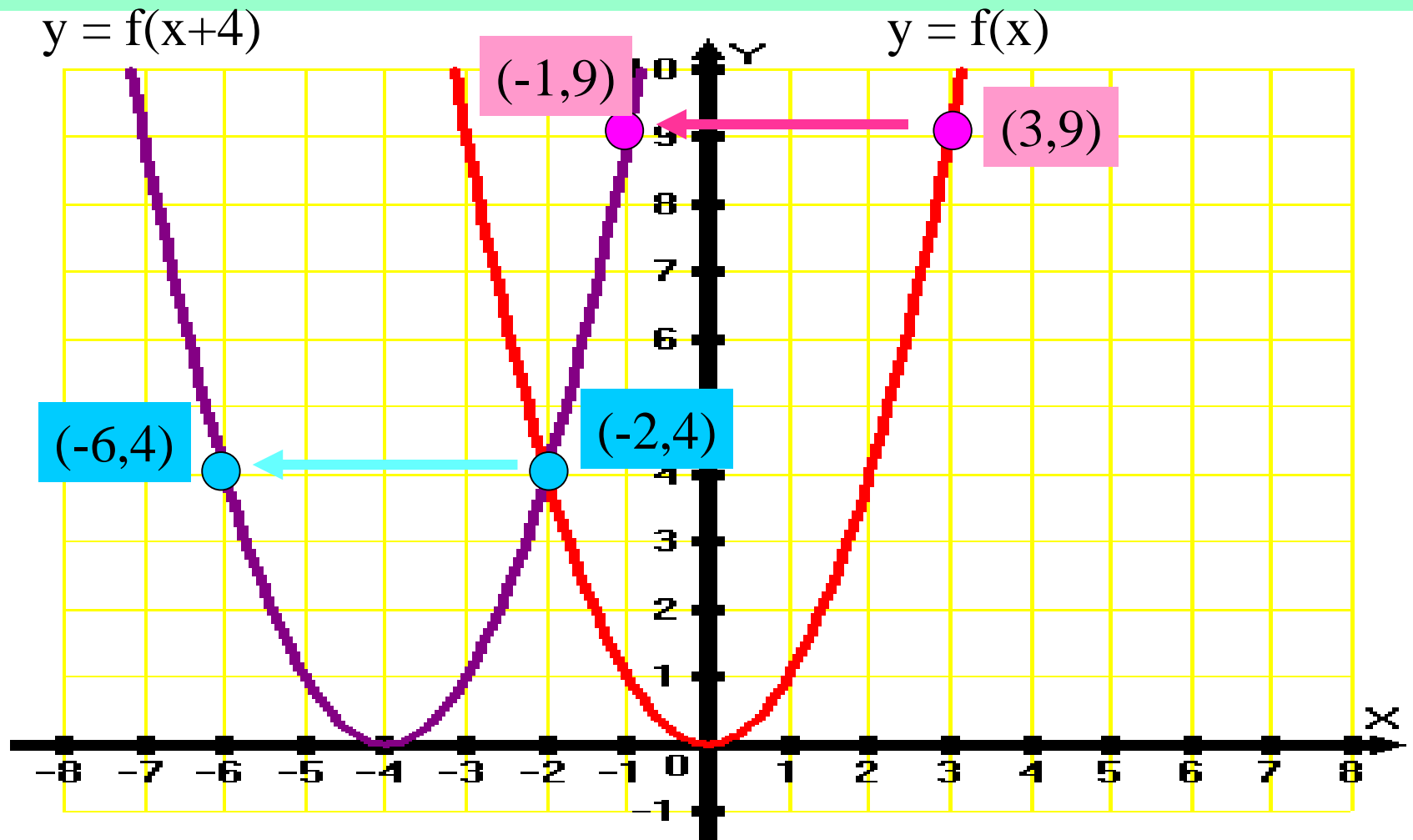
Lets look at what happens when we add a constant to the x values:

That is: $y = f(x) \rightarrow y = f(x + a)$

Starting again with the function $y = x^2$:

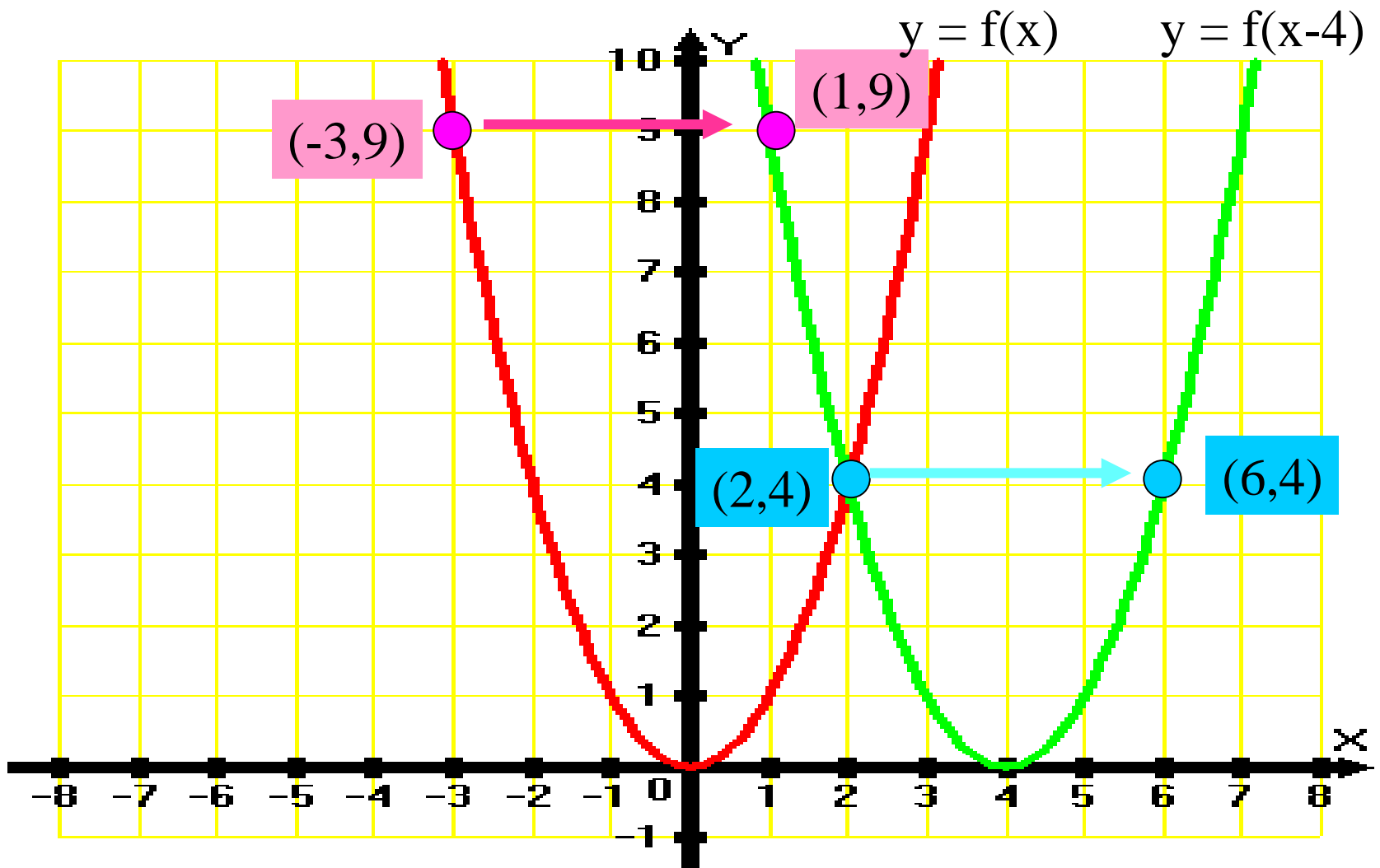


What will happen if we add 4 to each x value input ie. $y = (x+4)^2$?



EFFECT : 1. 4 has been subtracted from all x-coordinates
 2. Graph slides TO LEFT by 4

Will the effect be the same if we subtract 4 from x values?



EFFECT : 1. 4 has been added to all x-coordinates
2. Graph slides TO RIGHT by 4

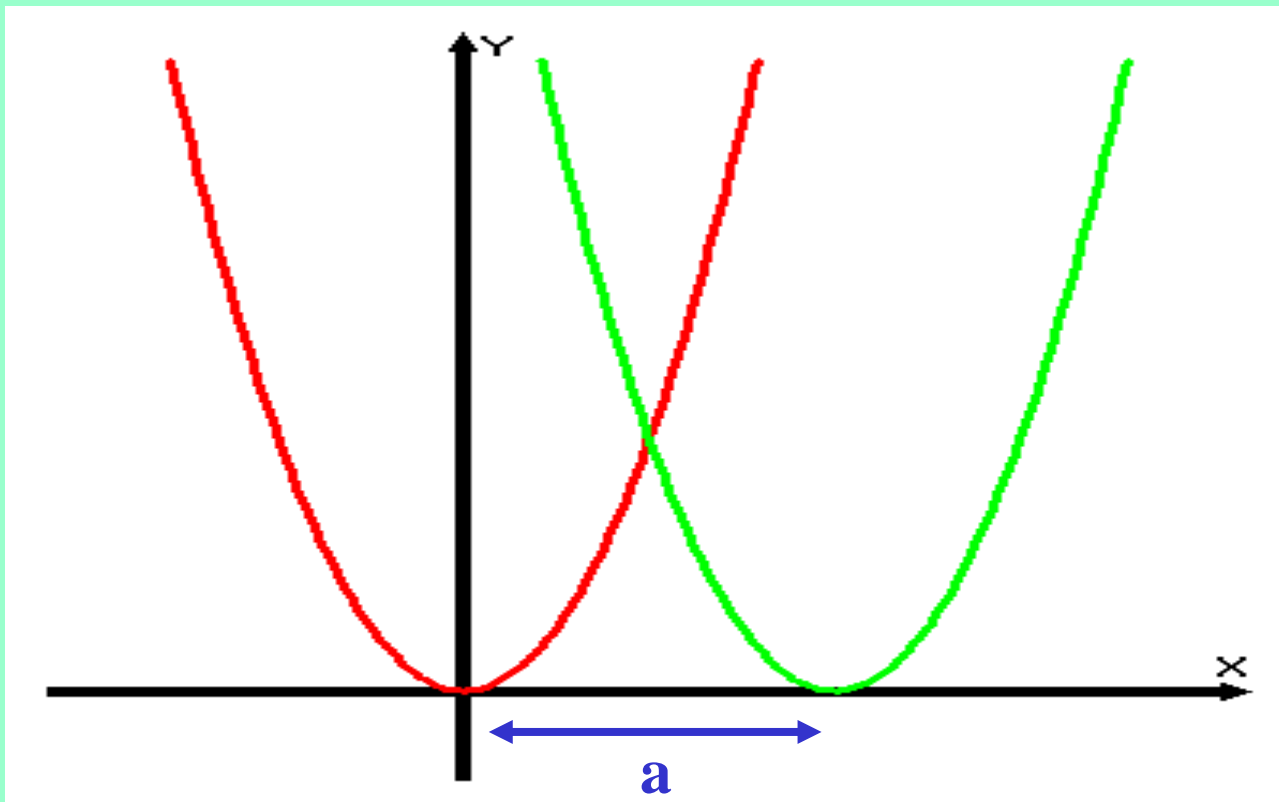
Graph of $y = f(x)+a$

Copy the following:

To obtain graph of $y = f(x+a)$ slide $y = f(x)$ horizontally by **a** units

To LEFT if a is positive

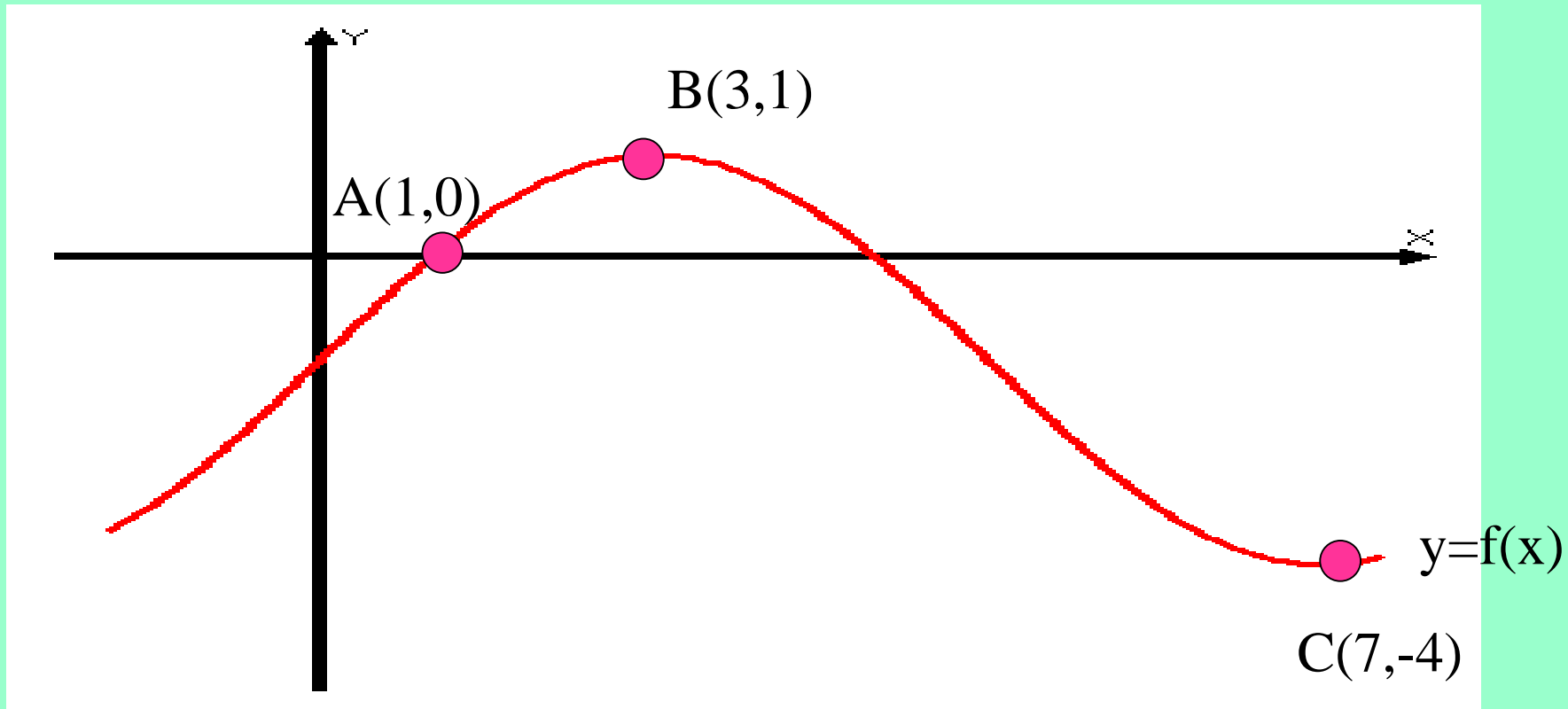
To RIGHT if a is negative



Example

Shown is the graph of $f(x)$.

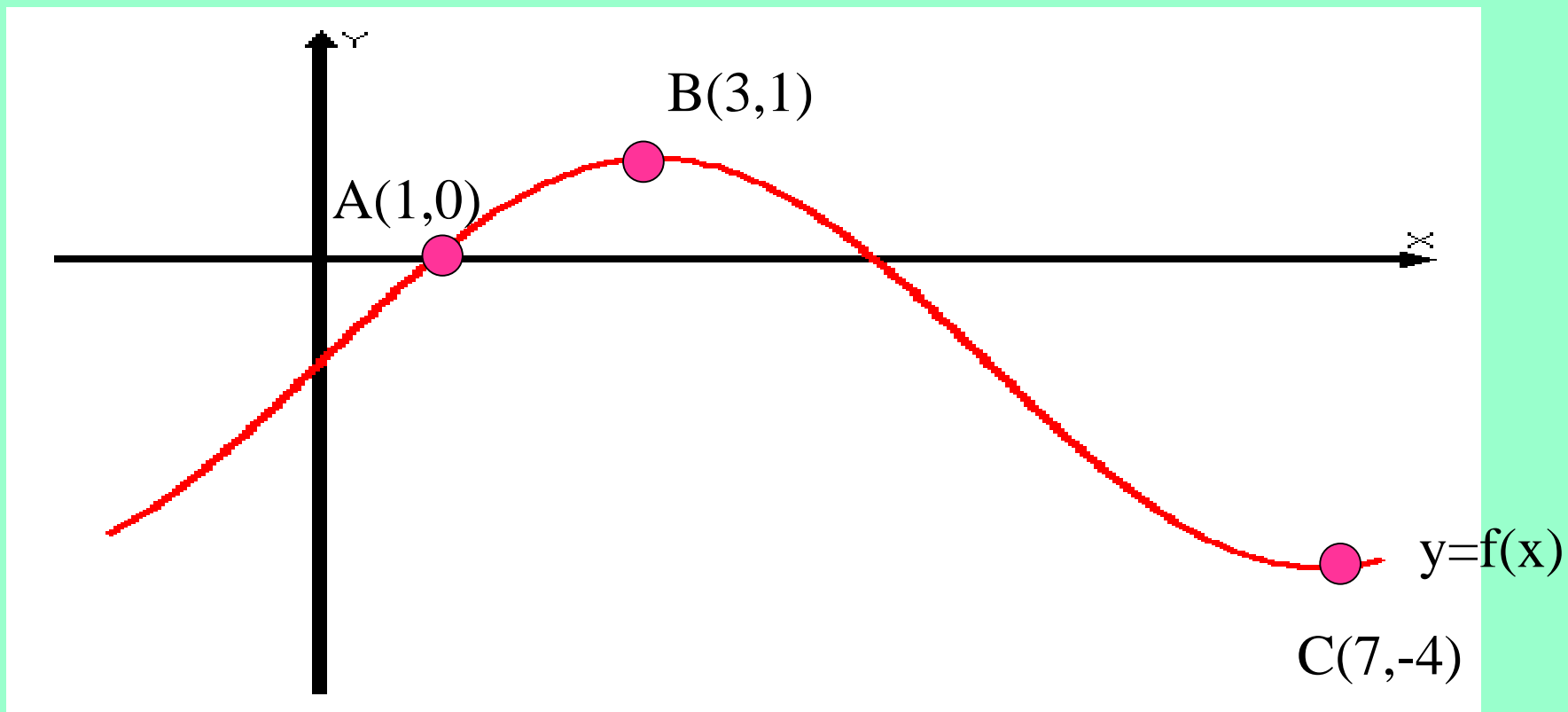
Sketch the graph of $f(x+2)$, clearly annotating the images of A, B and C.



Example

As required graph is $y = f(x + 2)$ we **subtract 2** from each x-coordinate.

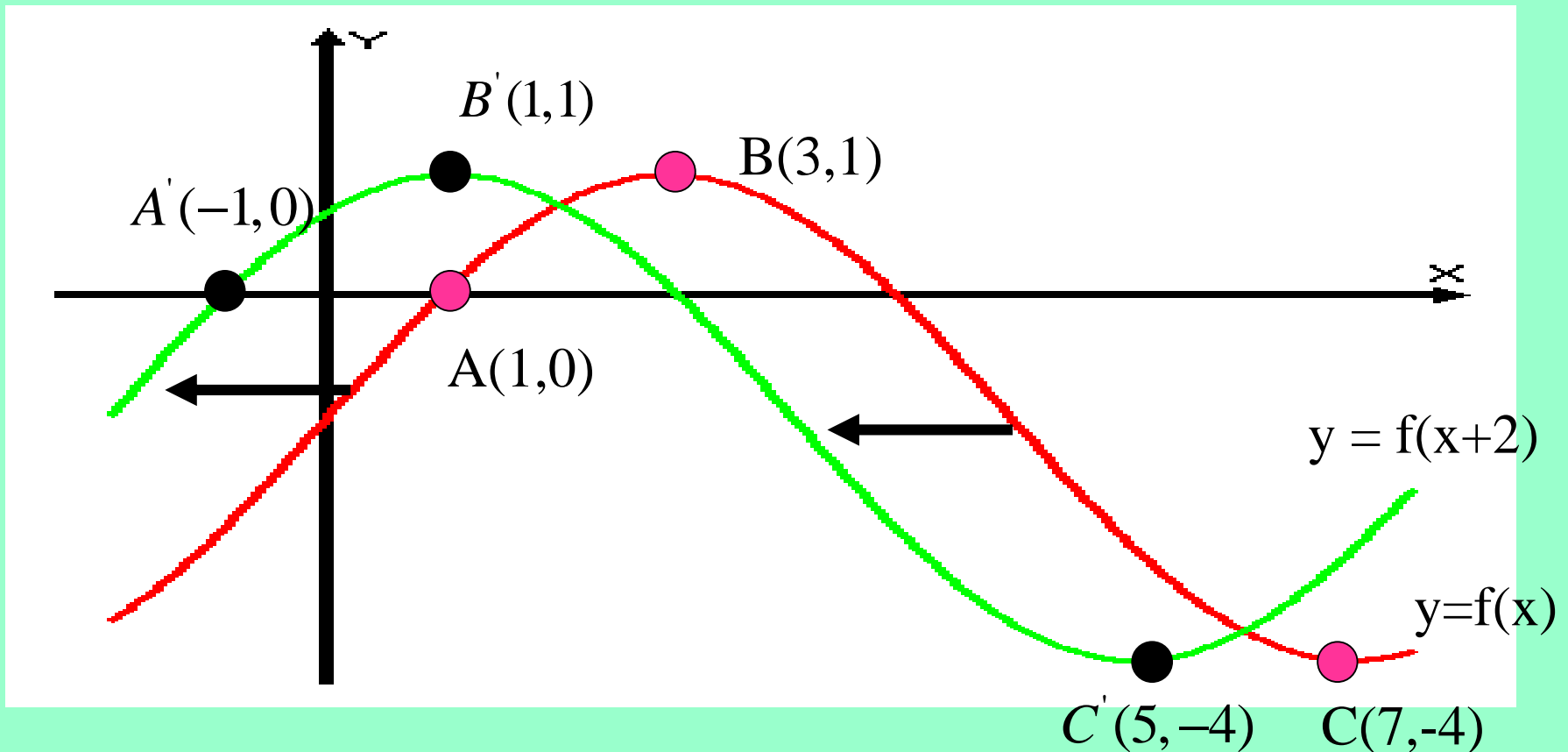
$$A(1,0) \rightarrow A'(-1,0) \quad B(3,1) \rightarrow B'(1,1) \quad C(7,-4) \rightarrow C'(5,-4)$$



Solution:

As required graph is $y = f(x + 2)$ we **subtract 2** to each x-coordinate.

$$A(1,0) \rightarrow A'(-1,0) \quad B(3,1) \rightarrow B'(1,1) \quad C(7,-4) \rightarrow C'(5,-4)$$



Heinemann, p.38, Ex 3E,
Q3 & 4