

5.

Special Lines

Horizontal Lines, Vertical Lines and
Lines through the Origin

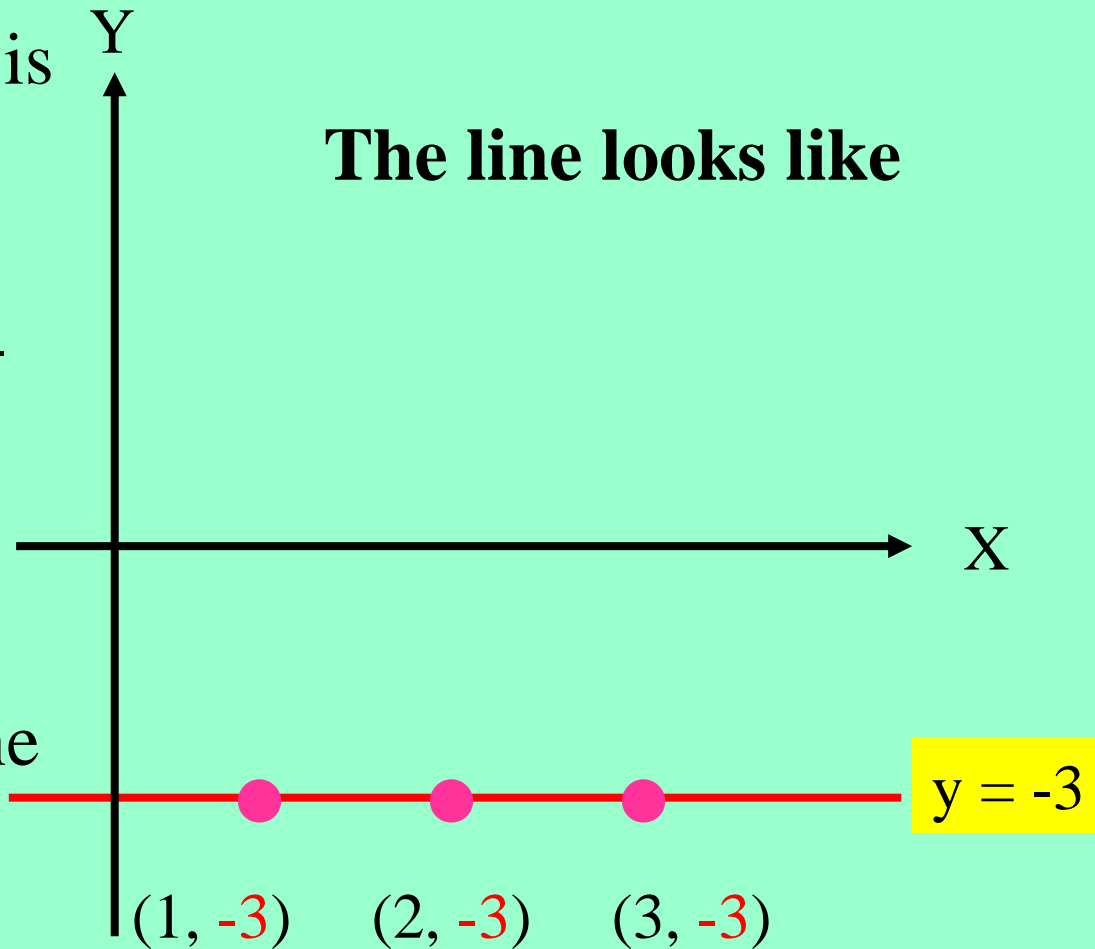


Equations of Lines

- Every line consists of a set of points which have some common property.
- This means that all the points on the line obey the same rule.
- This rule is called the equation of the line.
- The equation of a line is usually a formula connecting x and y .
- This tells us the connection between the \underline{x} -coordinate & \underline{y} -coordinate for each point on the line.

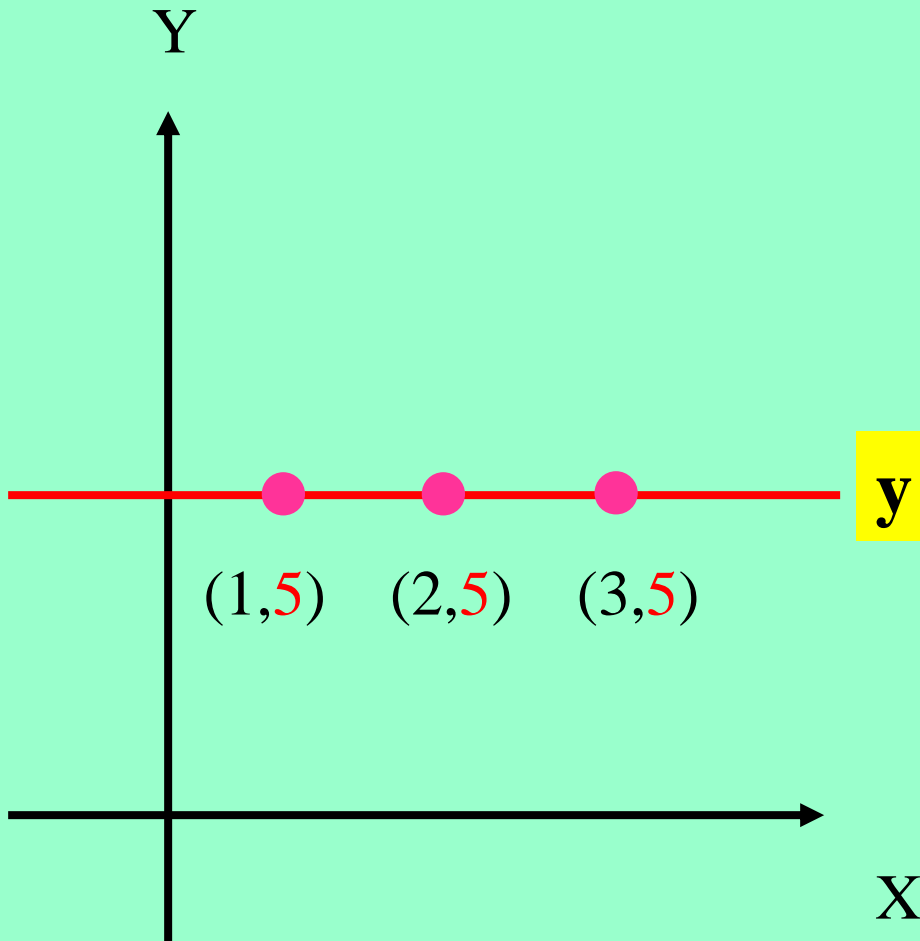
Horizontal Lines

- Every horizontal line is in the form $y = k$.
- This is because each point has the same y -coordinate.
- Consider the line $y = -3$
- Every point on the line has a y -coord of -3



Example

Sketch the graph of $y = 5$

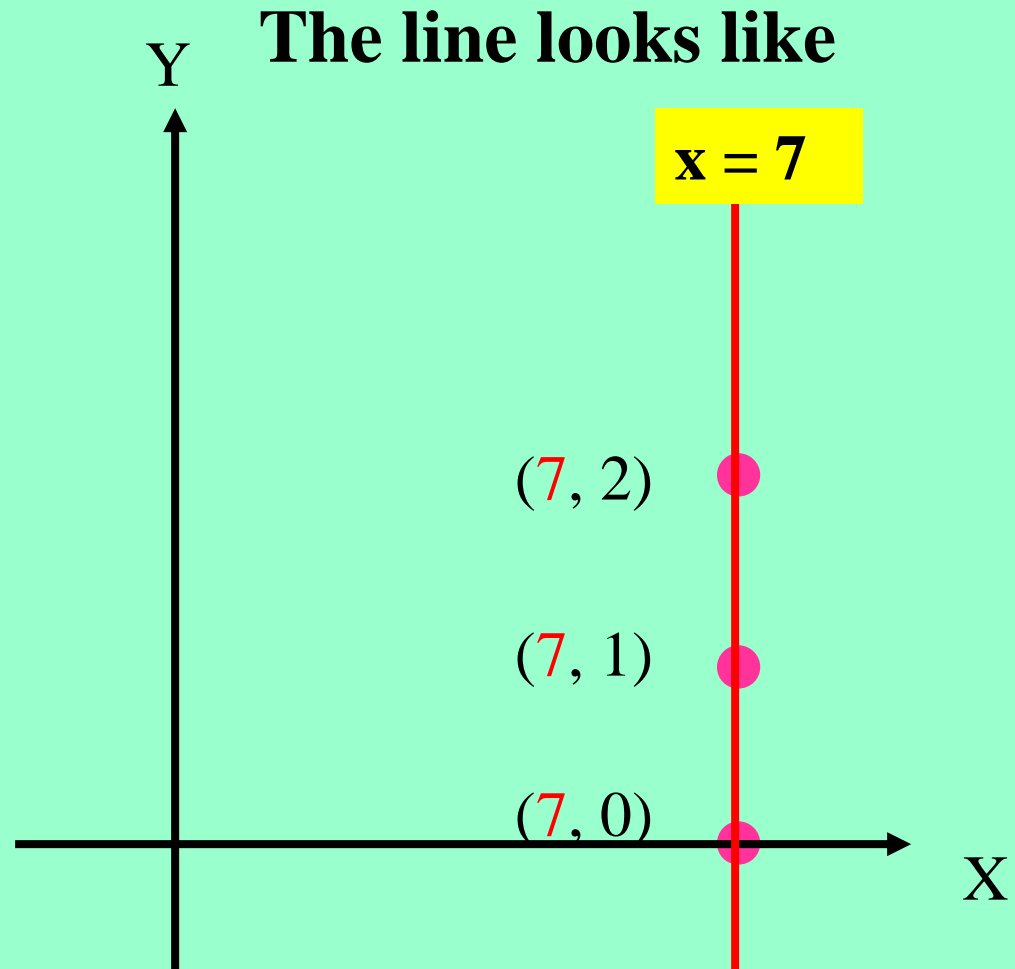


Every point on the line has a y-coordinate of 5 so the line is called

$$\underline{y = 5}$$

Vertical Lines

- Every vertical line is in the form $x = k$.
- This is because each point has the same x -coordinate.
- Consider the line $x = 7$
- Every point on the line has an x -coord of 7

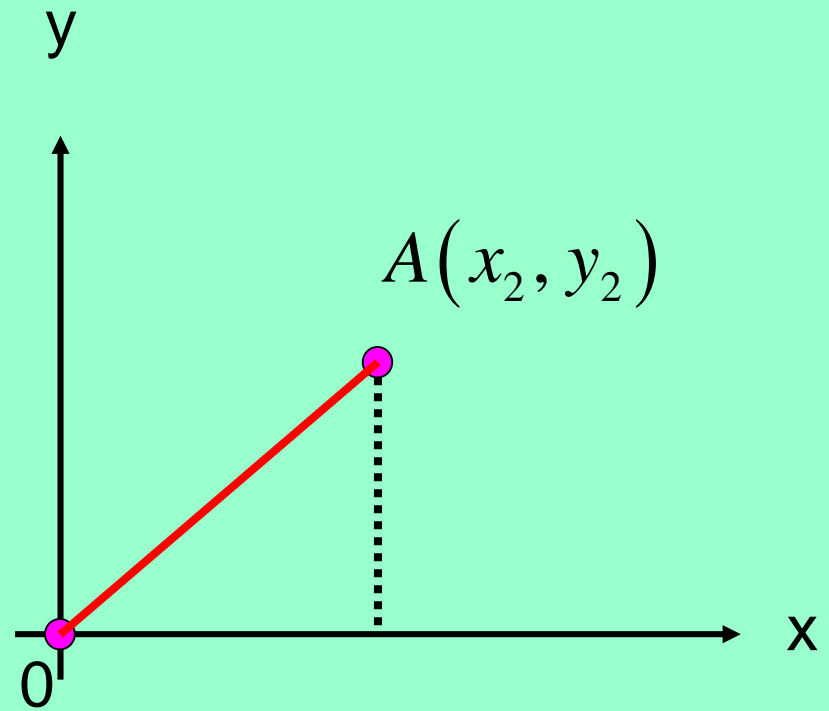


Lines through the Origin

To find the equation of a line through the origin:

Using our formula for gradients:

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{y_2 - 0}{x_2 - 0} = \frac{y_2}{x_2}$$



As line goes through Origin, Intercept is 0.

So

$$y = mx = \frac{y_2}{x_2} x$$

Example 1

Find the equation of OP, where O is the origin and P is the midpoint of Q (4, 6) and R (10, 10)

$$(x_1, y_1)$$

$$(x_2, y_2)$$

Solution :

1. Find P, midpoint of QR:

$$P\left(\frac{10+4}{2}, \frac{10+6}{2}\right) \longrightarrow P(7, 8)$$

2. Point through O so use
 $y = mx$

$$y = \frac{y_2}{x_2} x = \frac{8}{7} x$$

$$y = \frac{8}{7} x$$

Homework Booklet, EX 5 (ALL)