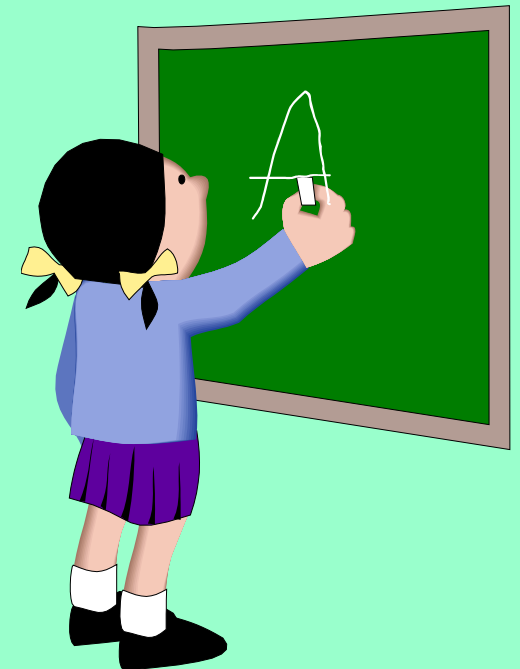
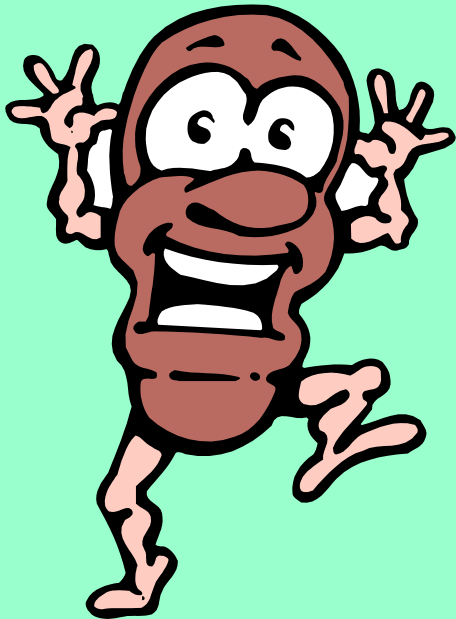


2.

Applications of the Addition Formulae



Example 1

By expressing 15° as $(60 - 45)^\circ$, find the **exact value** of $\sin 15^\circ$

Solution:

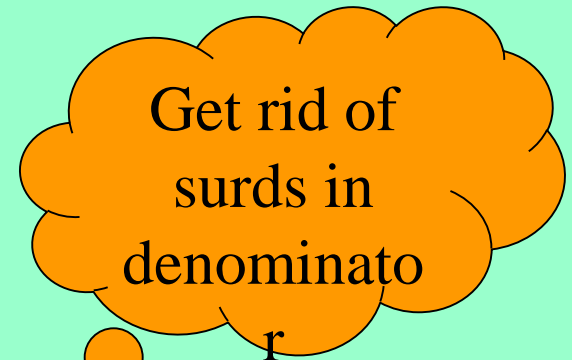
$$\sin 15^\circ = \sin(60 - 45)^\circ \quad \leftarrow \text{Rule 1(b)}$$

$$= \sin 60^\circ \cos 45^\circ - \cos 60^\circ \sin 45^\circ$$

$$= \frac{\sqrt{3}}{2} \cdot \frac{1}{\sqrt{2}} - \frac{1}{2} \cdot \frac{1}{\sqrt{2}}$$

$$= \frac{\sqrt{3}}{2\sqrt{2}} - \frac{1}{2\sqrt{2}}$$

$$= \frac{\sqrt{3} - 1}{2\sqrt{2}} \quad \leftarrow \quad \times \frac{\sqrt{2}}{\sqrt{2}}$$



Example 1

By expressing 15° as $(60 - 45)^\circ$, find the **exact value** of $\sin 15^\circ$

Solution:

$$\sin 15^\circ = \sin(60 - 45)^\circ \quad \leftarrow \text{Rule 1(b)}$$

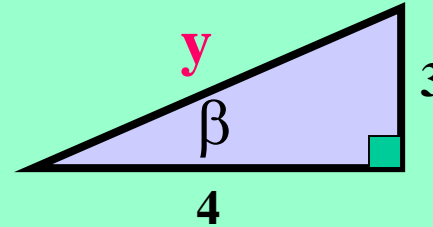
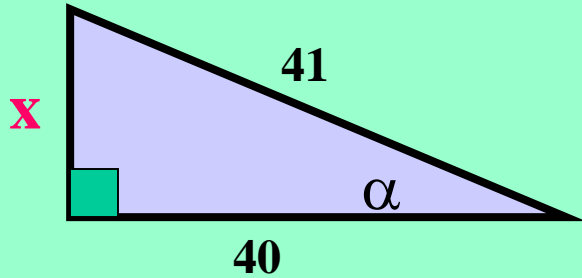
$$= \frac{\sqrt{3} - 1}{2\sqrt{2}} \quad \leftarrow \times \frac{\sqrt{2}}{\sqrt{2}}$$

$$= \frac{\sqrt{6} - \sqrt{2}}{2 \times 2}$$

$$= \frac{\sqrt{6} - \sqrt{2}}{4} \quad \rightarrow \quad = \frac{1}{4}(\sqrt{6} - \sqrt{2})$$

Example 2

NAB



Show that $\cos(\alpha - \beta) = \frac{187}{205}$

Solution:

THINK:

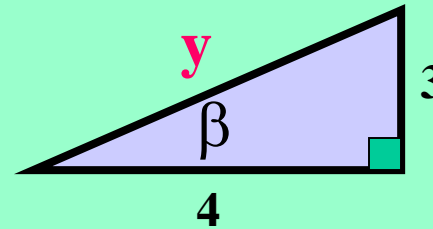
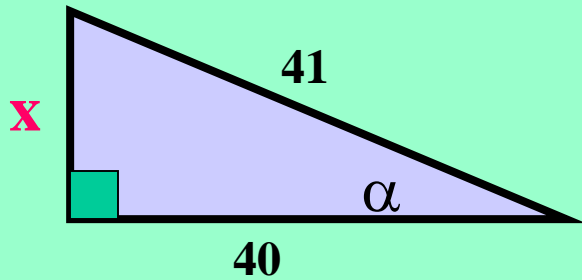
$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

NEED:

$$\cos \alpha = \frac{40}{41} \quad \cos \beta = \frac{4}{y} \quad \sin \alpha = \frac{x}{41} \quad \sin \beta = \frac{3}{y}$$

Example 2

NAB



Show that $\cos(\alpha - \beta) = \frac{187}{205}$

Solution:

BY PYTHAG.

$$x^2 = 41^2 - 40^2$$

$$y^2 = 4^2 + 3^2$$

$$x = \sqrt{81}$$

$$y = \sqrt{25}$$

$$x = 9$$

$$y = 5$$

NEED:

$$\cos \alpha = \frac{40}{41}$$

$$\cos \beta = \frac{4}{y}$$

$$\sin \alpha = \frac{x}{41}$$

$$\sin \beta = \frac{3}{y}$$

$$\cos(\alpha - \beta) = \cos\alpha\cos\beta + \sin\alpha\sin\beta$$

$$= \left(\frac{40}{41} \times \frac{4}{5}\right) + \left(\frac{9}{41} \times \frac{3}{5}\right)$$

$$= \frac{160}{205} + \frac{27}{205}$$

$$= \frac{187}{205}$$

NEED:

$$\cos \alpha = \frac{40}{41}$$

$$\cos \beta = \frac{4}{5}$$

$$\sin \alpha = \frac{9}{41}$$

$$\sin \beta = \frac{3}{5}$$

Heinemann,
p.189, EX 11B, Q3 & 5,
p. 190, EX 11C, Q3 & 6,
p.191, EX 11D, Q4, 5 & 7