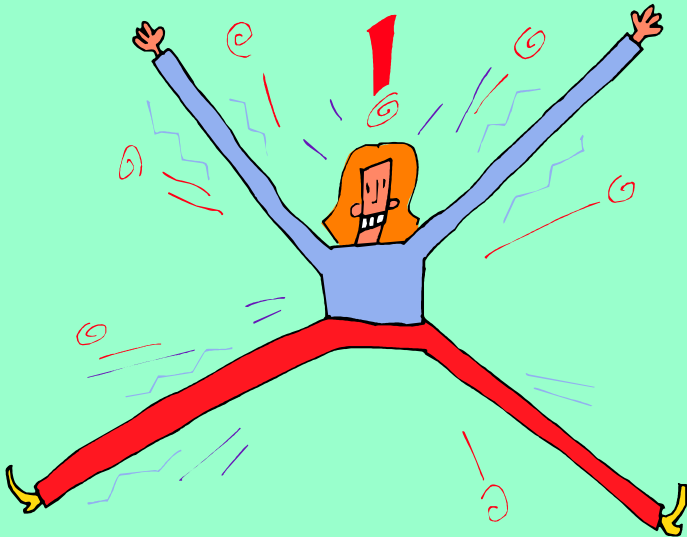


12.

Graph of $kf(x)$

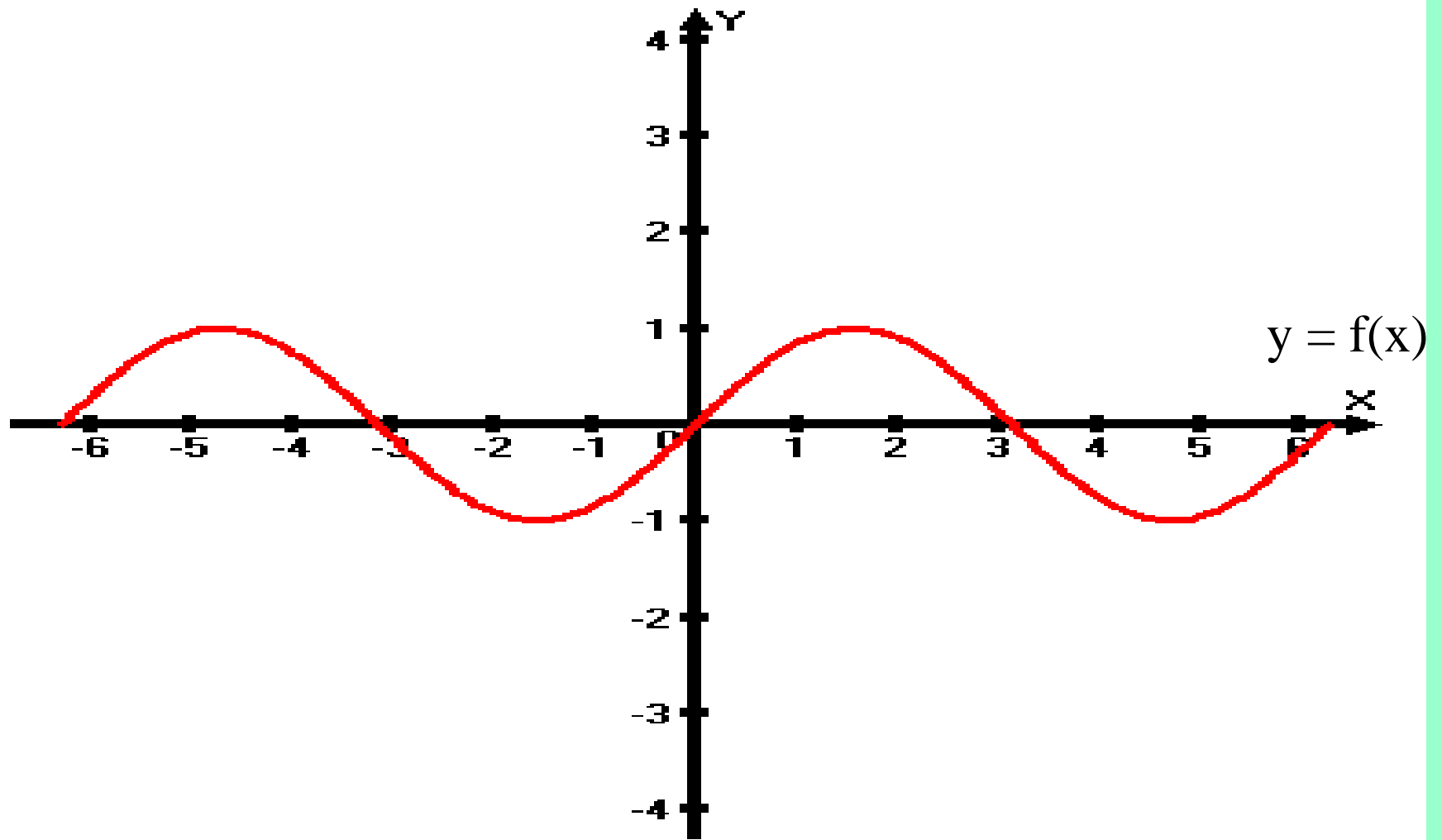


Graph of $kf(x)$

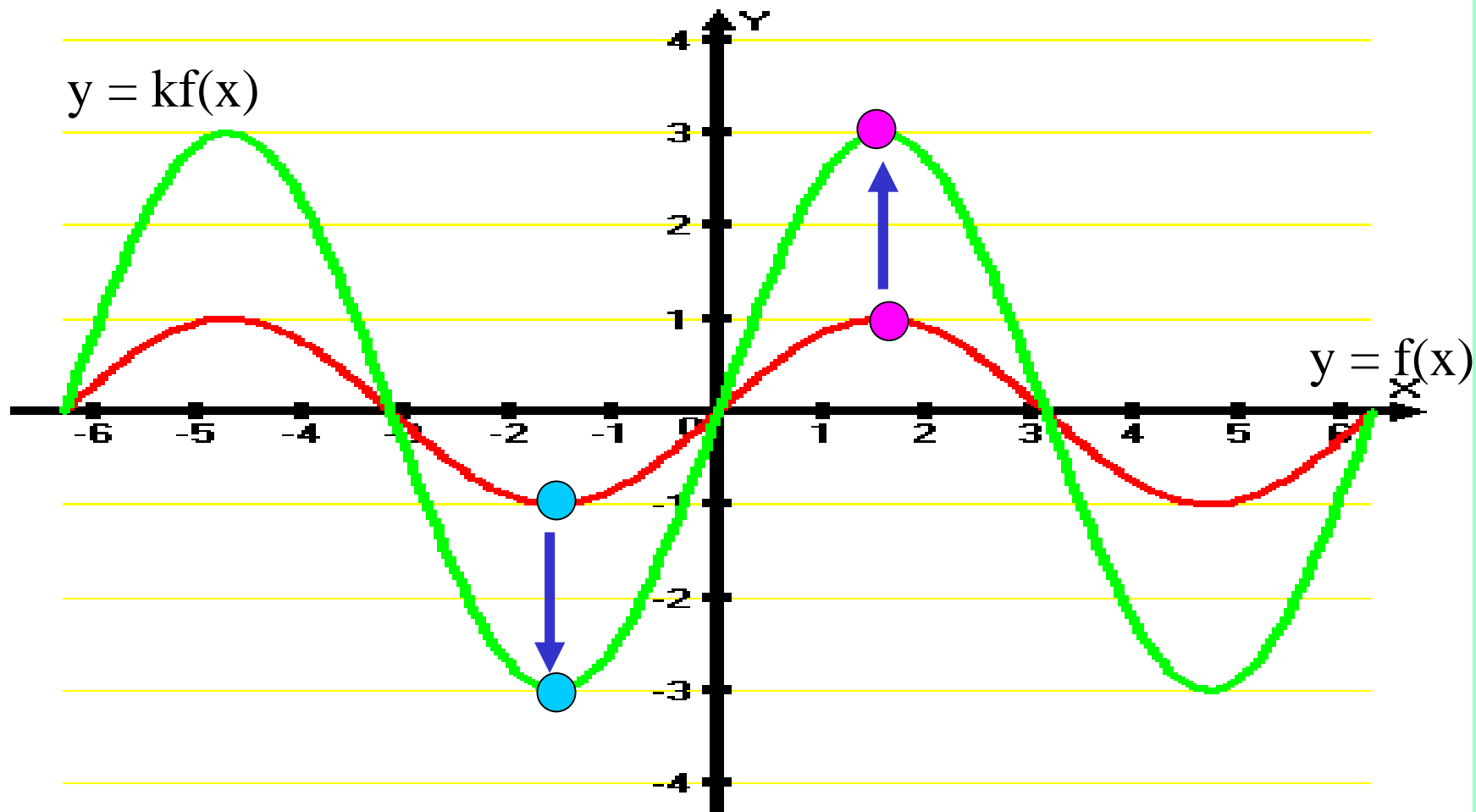
We are now going to look at what happens to $f(x)$ if we multiply the whole function by a given value.

That is: $y = f(x) \rightarrow y = kf(x)$

This time we will start with the function $y = \sin(x)$ as trig graphs illustrate the effects most clearly:



What will happen if we change this to $y = 3\sin(x)$?



EFFECT : The x-coordinates are unchanged for corresponding points but the y-coordinates have been multiplied by a factor of k. The graph has not moved left or right.

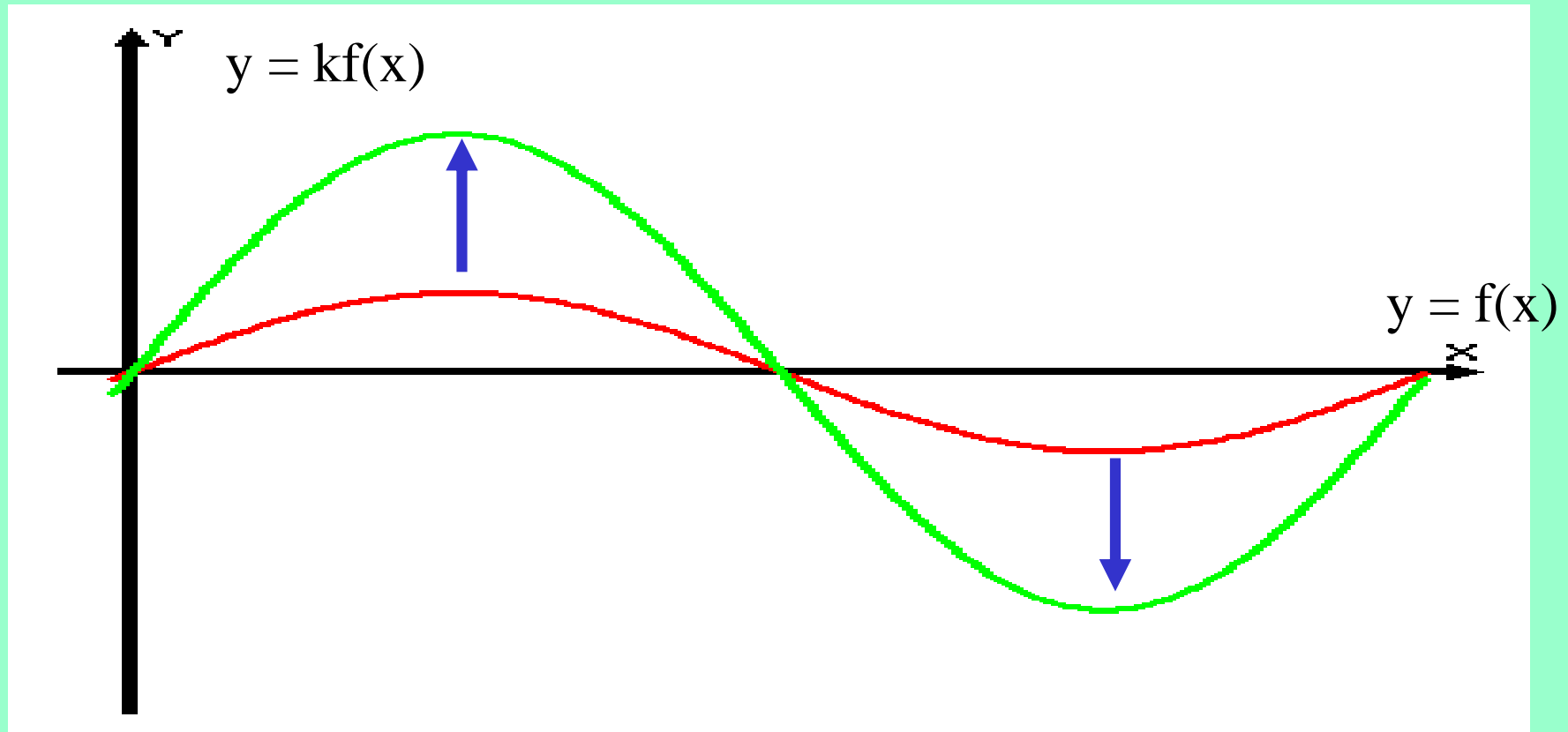
Graph of $y = k f(x)$

Copy the following:

To obtain graph of $y = k f(x)$ the graph is multiplied by a factor of k .

Multiply the y-coordinate by k : $(a, b) \rightarrow (a, kb)$

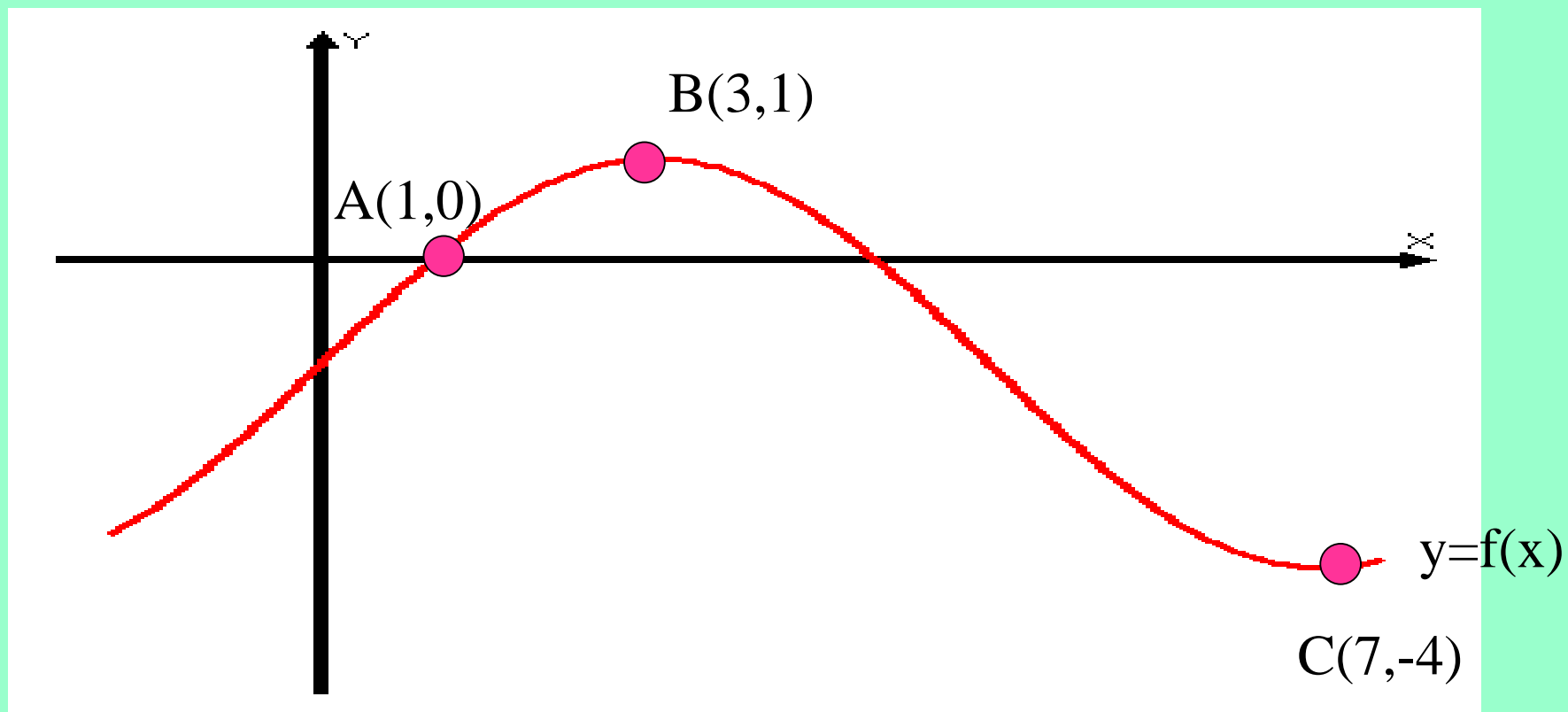
NOTE: If $k > 1$ then graph stretched If $k < 1$ then graph squashed



Example

Shown is the graph of $f(x)$.

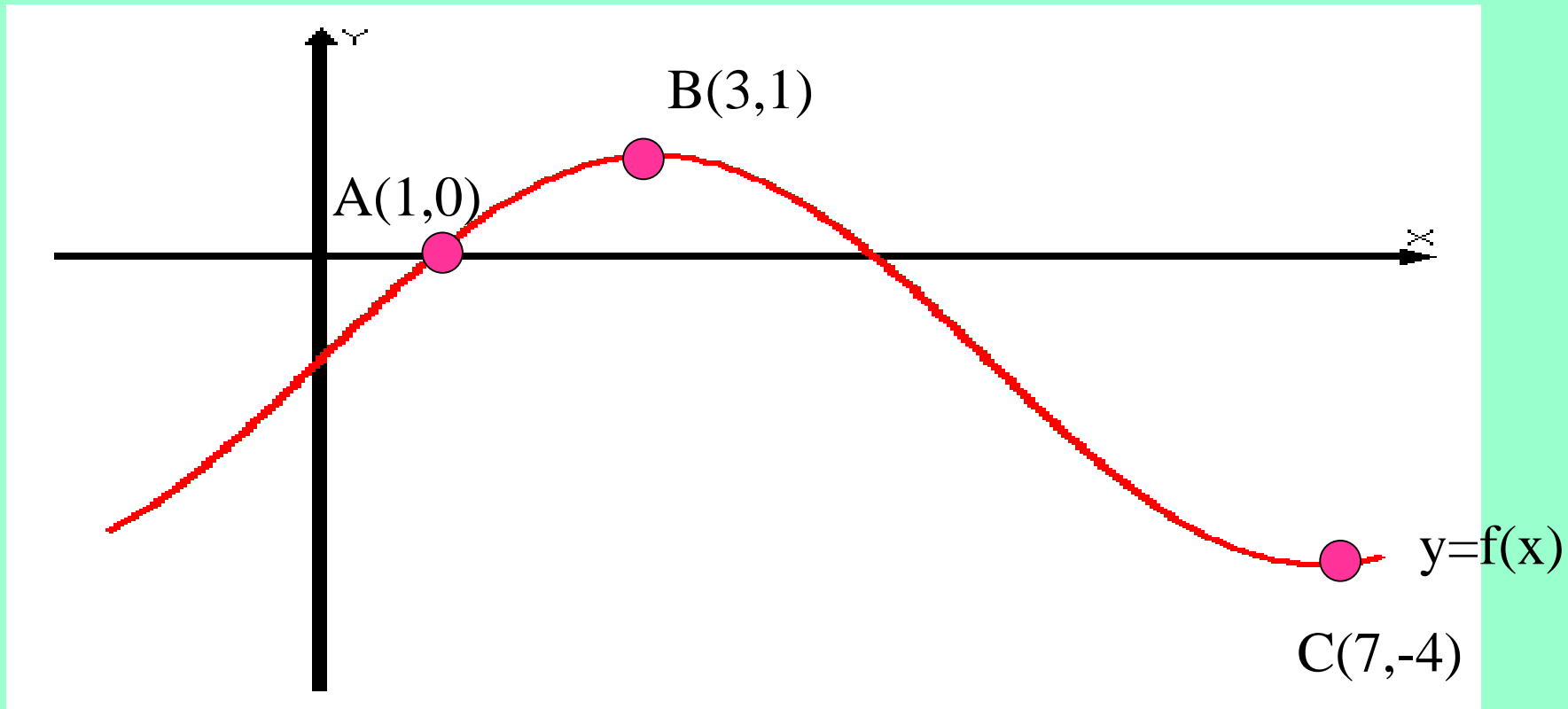
Sketch the graph of $2f(x)$, clearly annotating the images of A, B and C.



Solution:

As required graph is $y = 2f(x)$ we **multiply** each y-coordinate by 2.

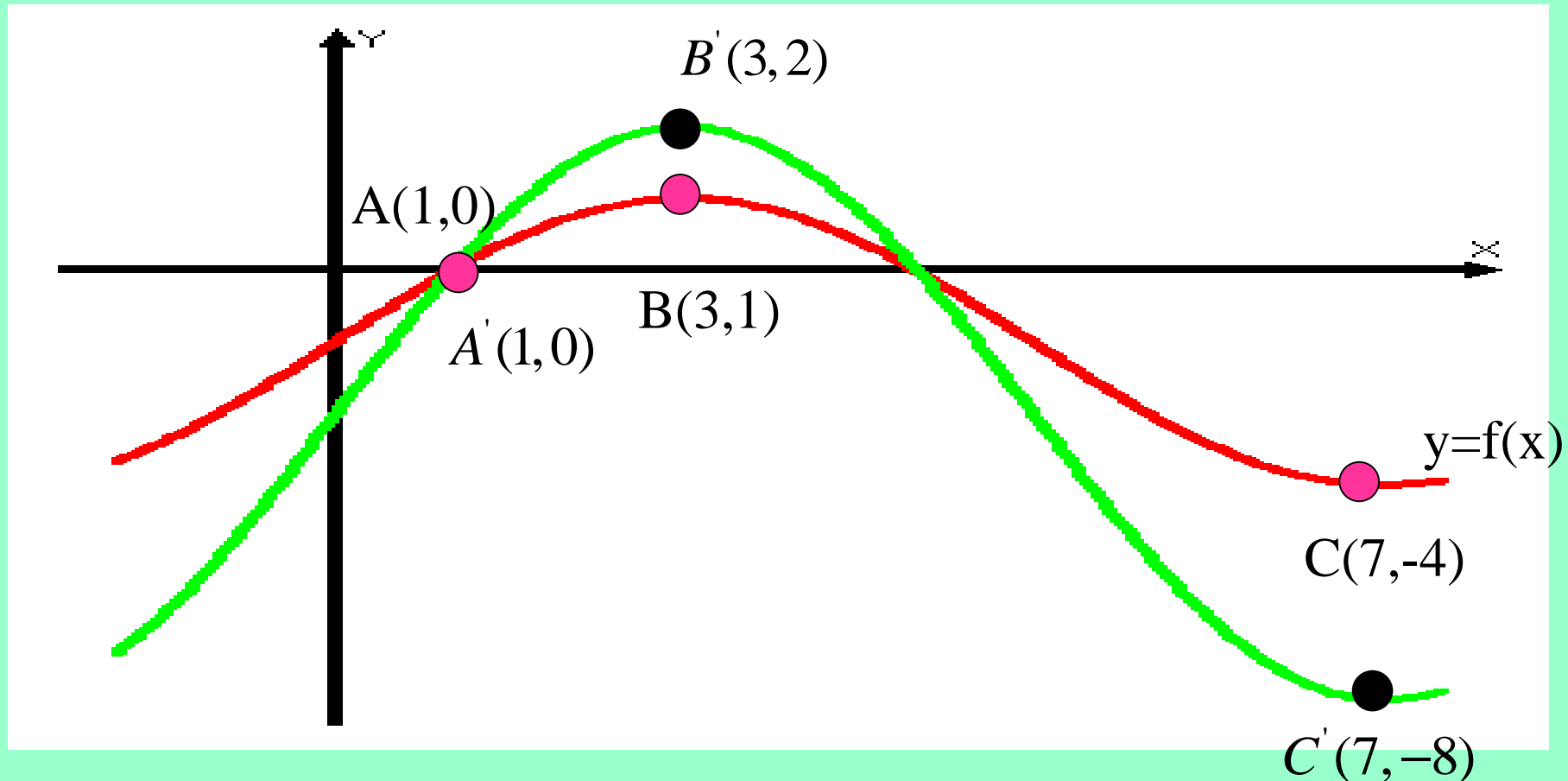
$$A(1,0) \rightarrow A'(1,0) \quad B(3,1) \rightarrow B'(3,2) \quad C(7,-4) \rightarrow C'(7,-8)$$



Solution:

As required graph is $y = 2f(x)$ we **multiply** each y-coordinate by 2.

$$A(1,0) \rightarrow A'(1,0) \quad B(3,1) \rightarrow B'(3,2) \quad C(7,-4) \rightarrow C'(-7,-8)$$



Heinemann, p.43, Ex 3K