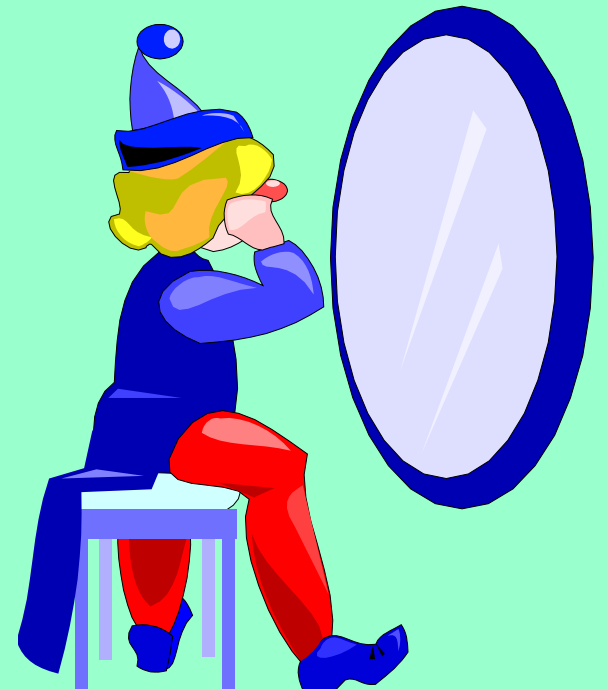


**10.**

Graph of  $-f(x)$

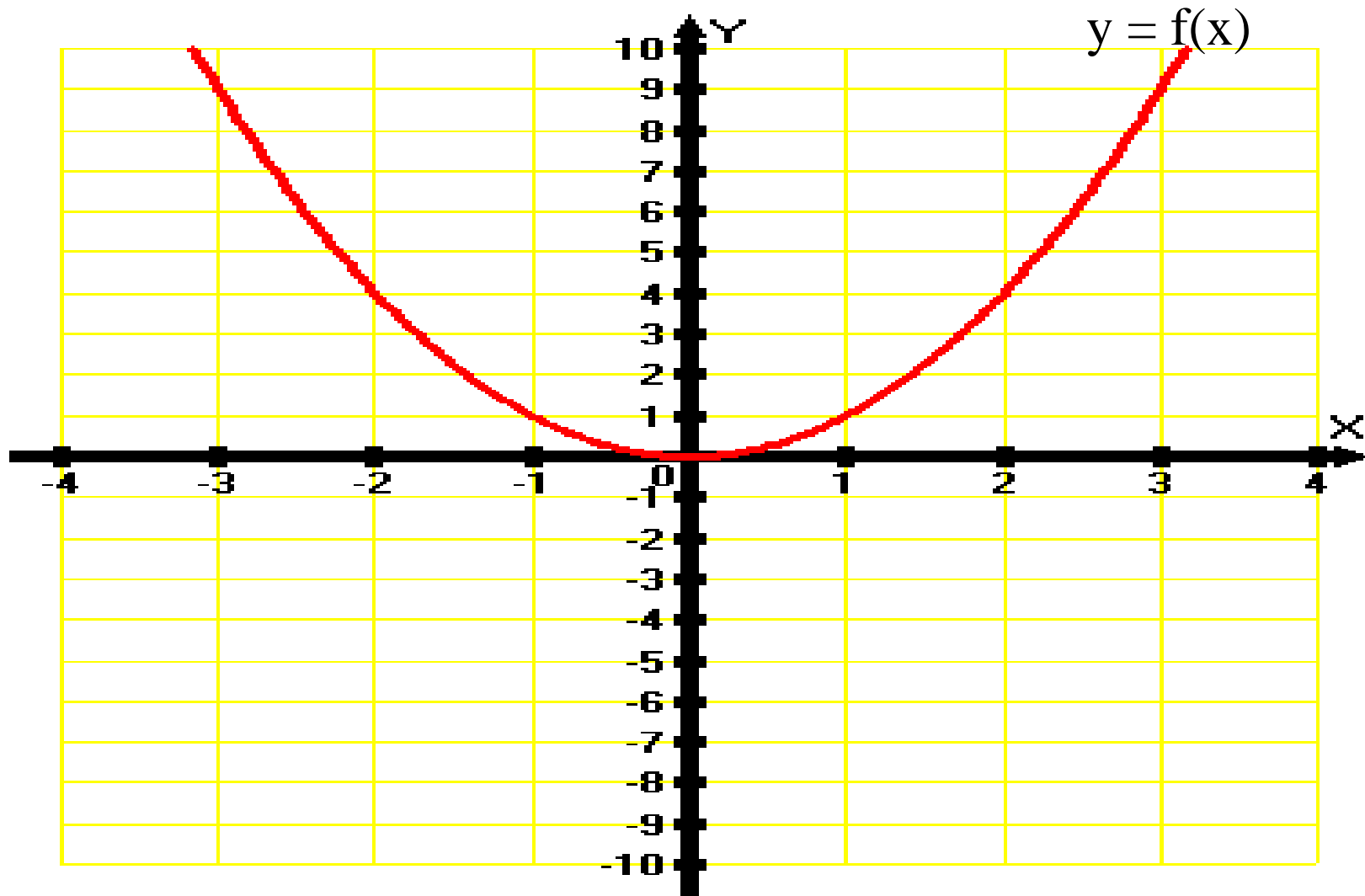


# Graph of $-f(x)$

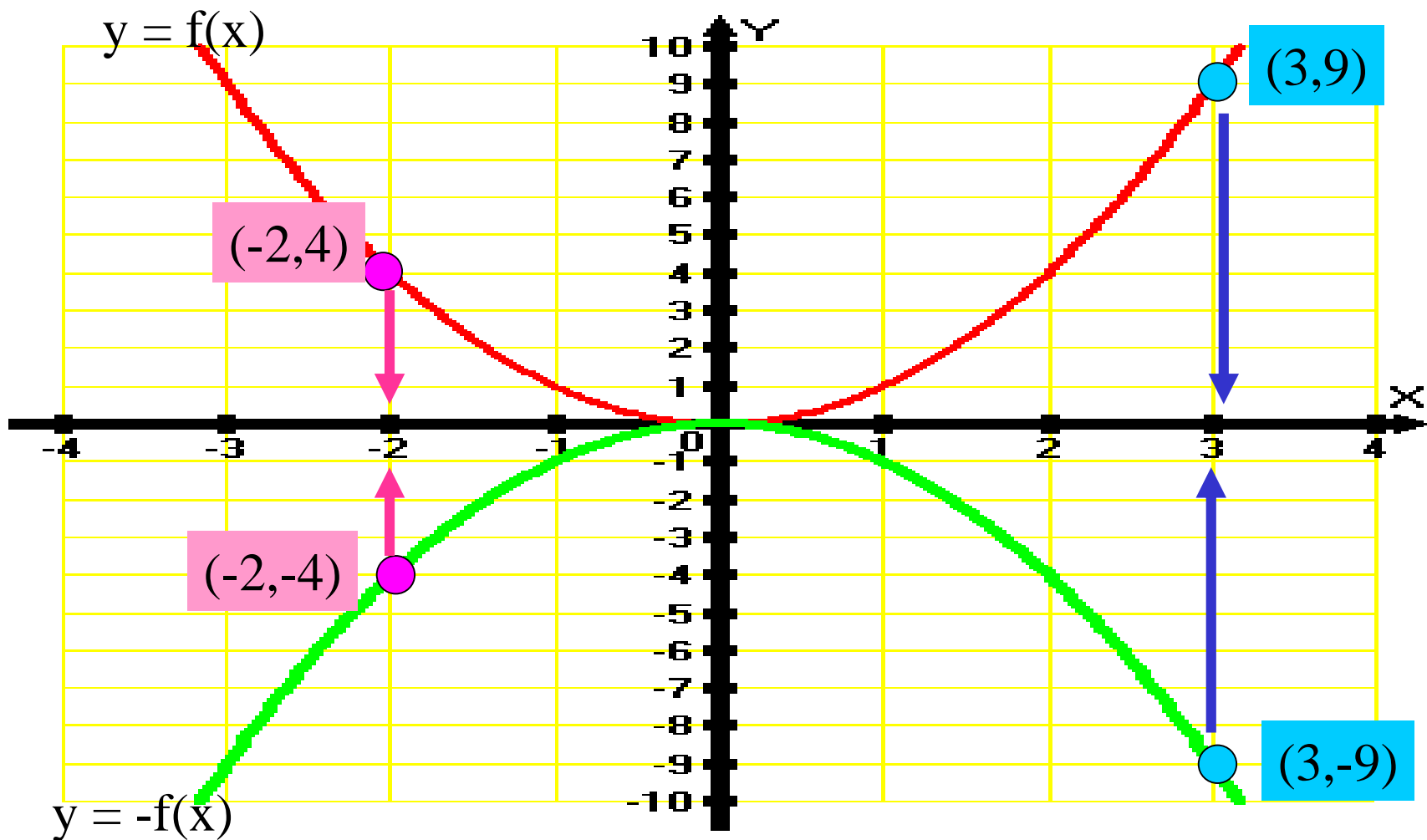
We are now going to look at what happens to  $f(x)$  if we change the polarity (change the sign) of the  $y$ -values.

That is:  $y = f(x) \rightarrow y = -f(x)$

Once again we will start with the function  $y = x^2$  :



What will happen if we change this to  $y = -(x)^2$  ?



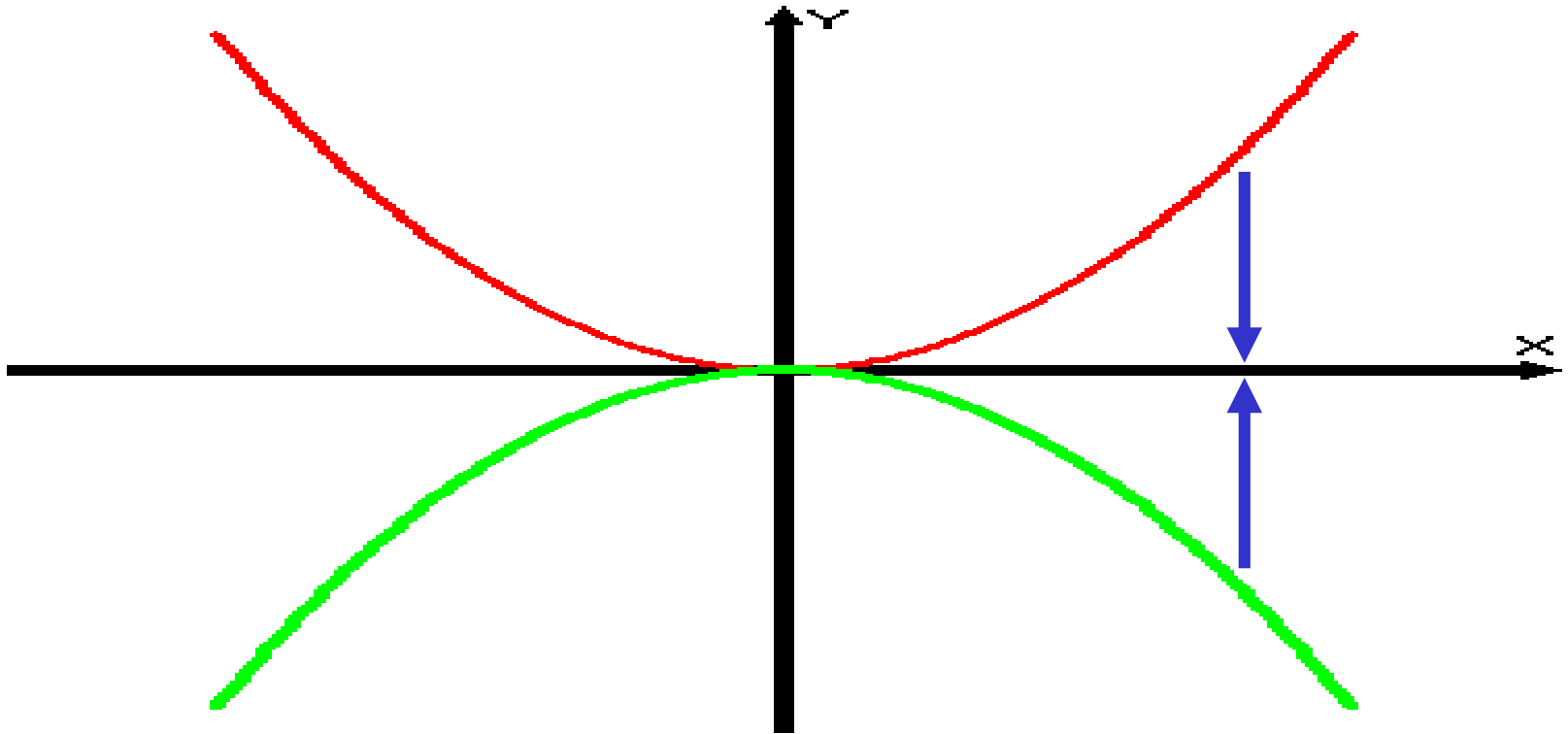
**EFFECT :** The graph has been turned upside down.  
This occurs by reflecting  $f(x)$  in the x-axis.  
As a result the y-coordinate of each point changes sign.

## Graph of $y = -f(x)$

Copy the following:

To obtain graph of  $y = -f(x)$  reflect  $y = f(x)$  in the x-axis

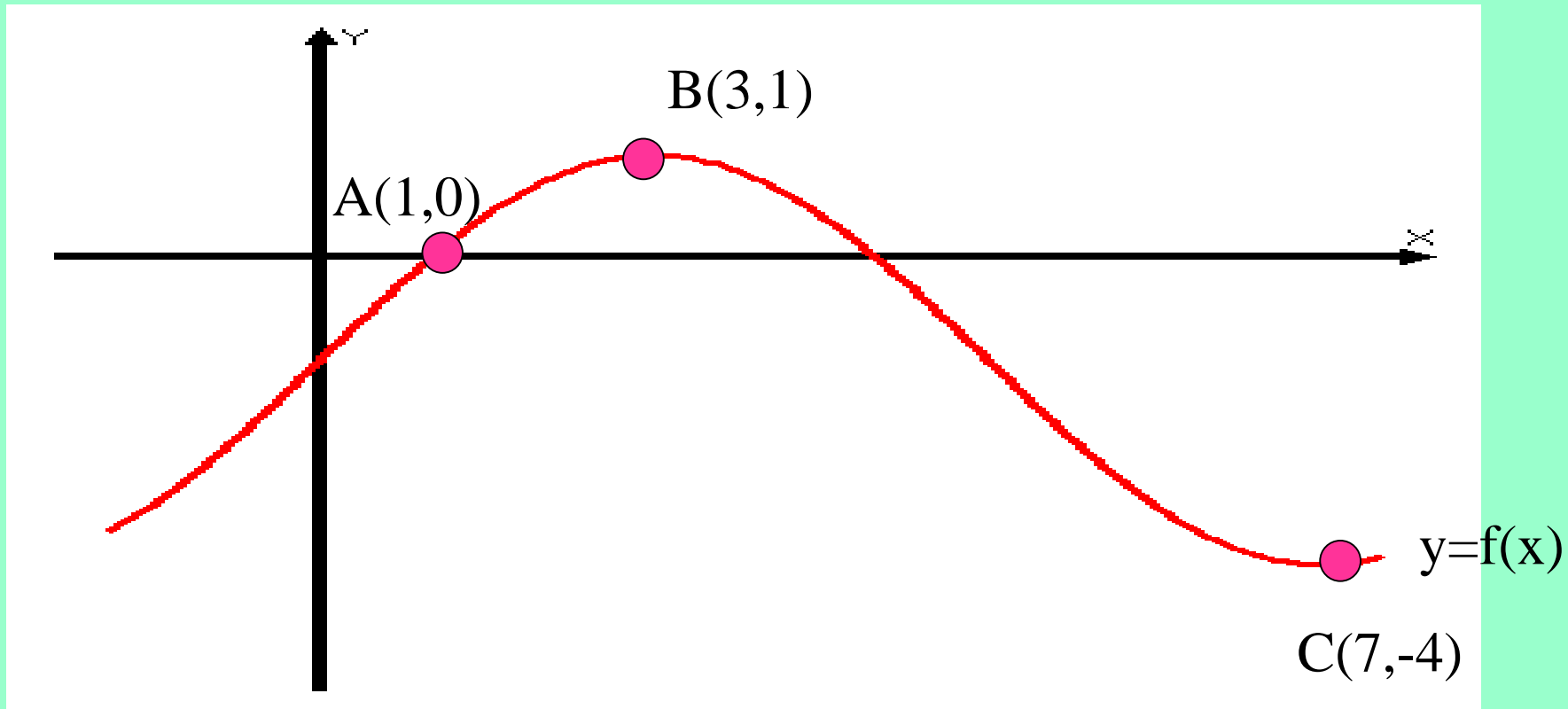
Change the sign of the y-coordinate so  $(a, b) \rightarrow (a, -b)$



## Example

Shown is the graph of  $f(x)$ .

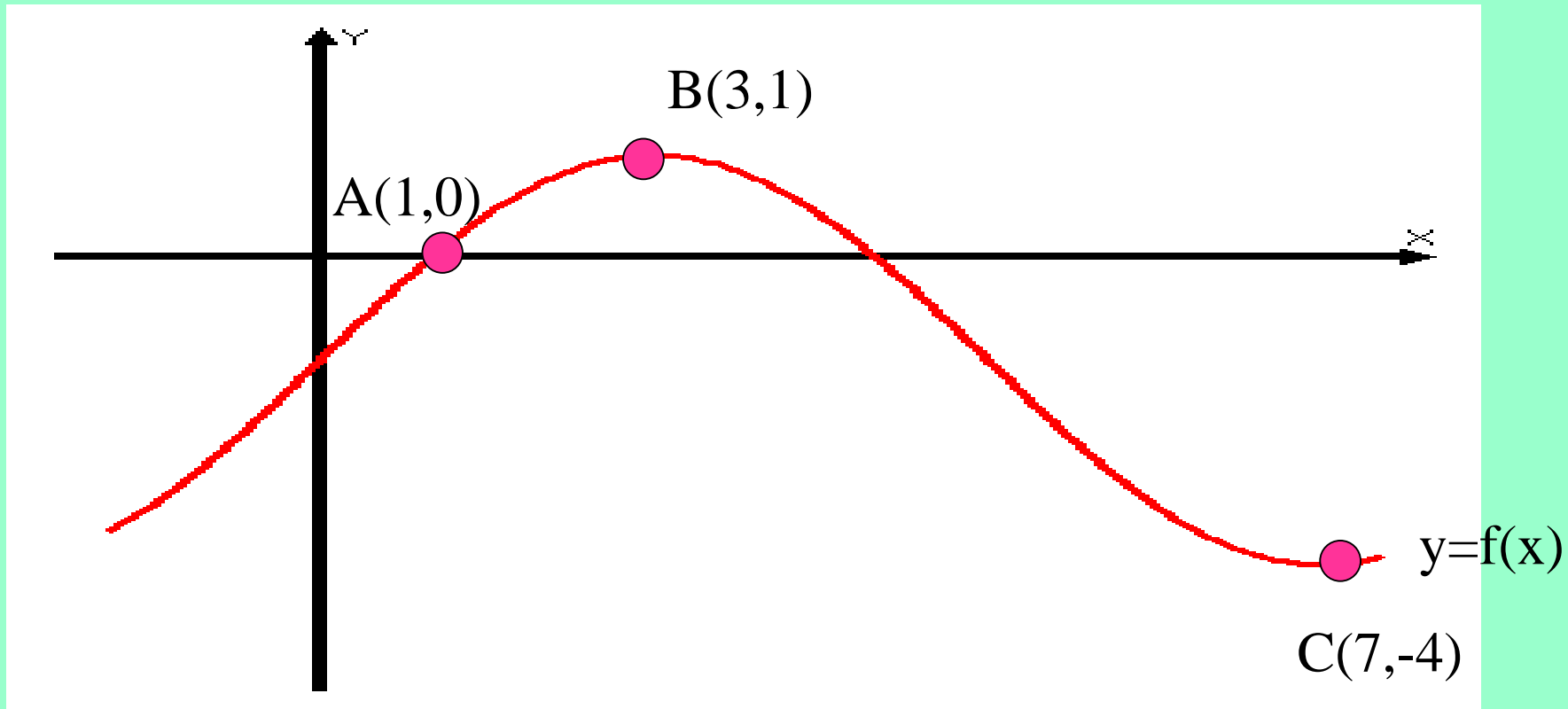
Sketch the graph of  $-f(x)$ , clearly annotating the images of A, B and C.



## Solution:

As required graph is  $y = -f(x)$  we **change sign** of each y-coordinate.

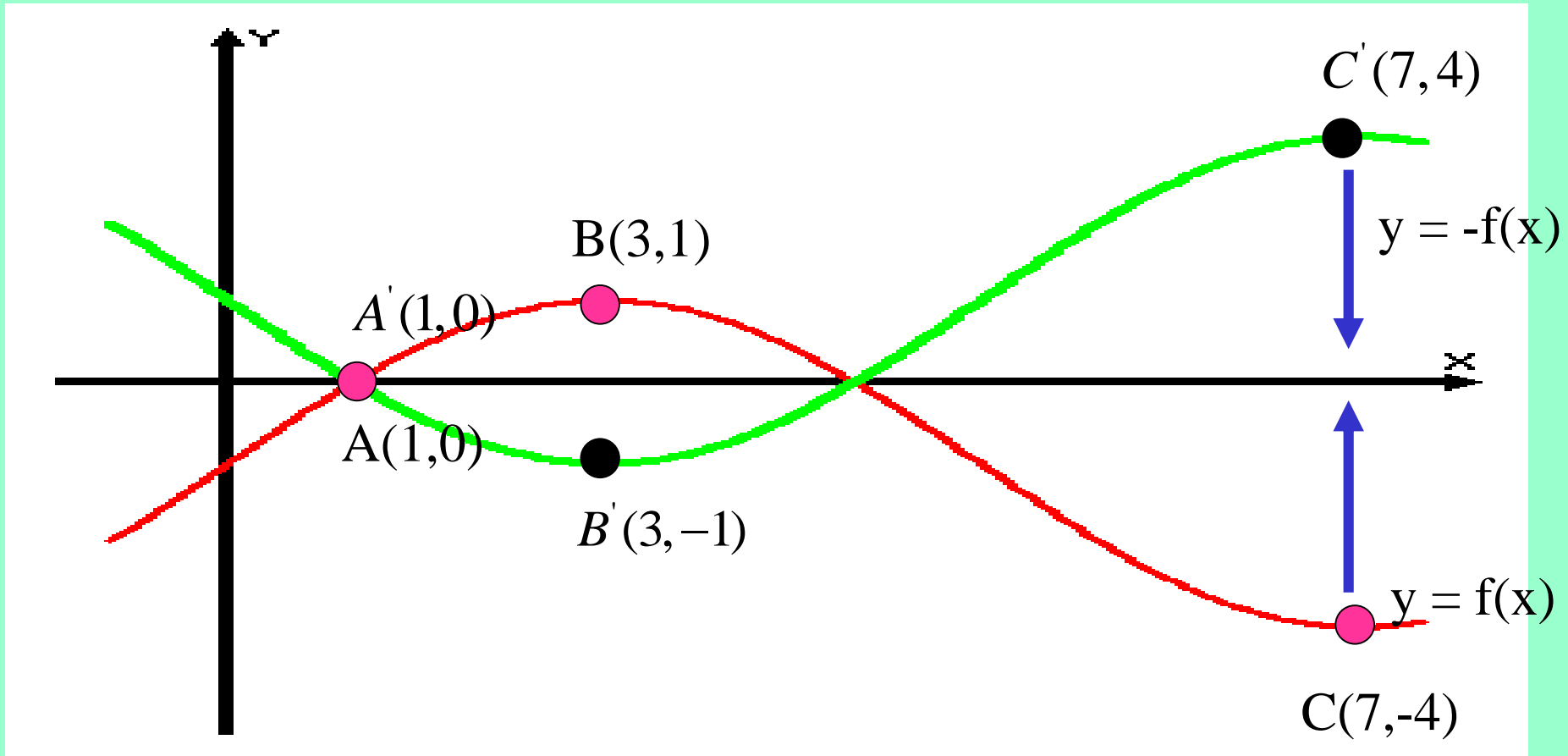
$$A(1,0) \rightarrow A'(1,0) \quad B(3,1) \rightarrow B'(3,-1) \quad C(7,-4) \rightarrow C'(7,4)$$



## Solution:

As required graph is  $y = -f(x)$  we change the sign of each y-coordinate

$$A(1,0) \rightarrow A'(1,0) \quad B(3,1) \rightarrow B'(3,-1) \quad C(7,-4) \rightarrow C'(7,4)$$





Heinemann, p.40, Ex 3G, Q2, 3, 4